

Ontological formalisation of mathematical equations for phenomic data exploitation

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Seminar In-OVIVE

September, 2021

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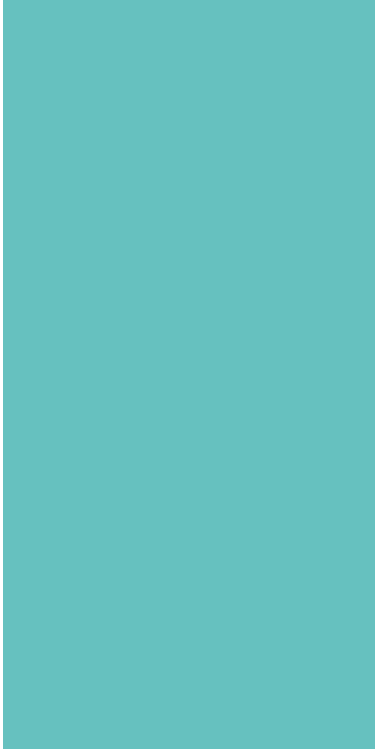
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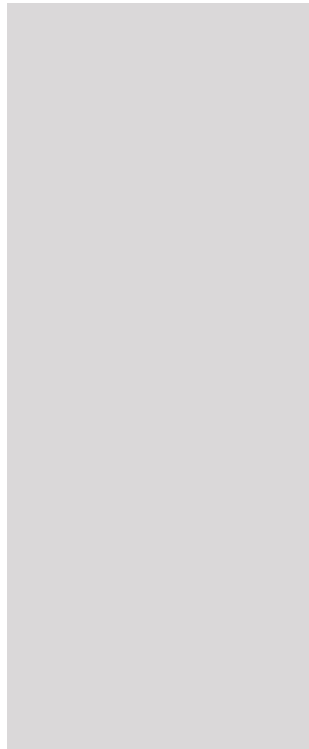
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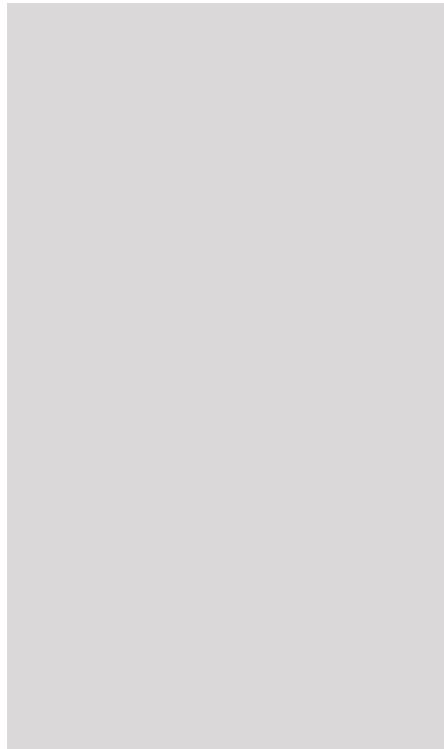
MOTIVATION



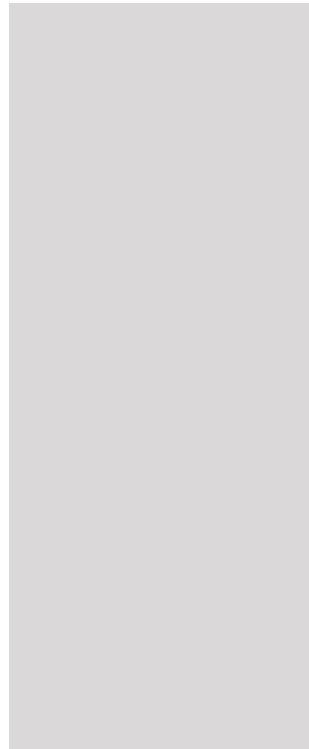
**RELATED
WORKS**



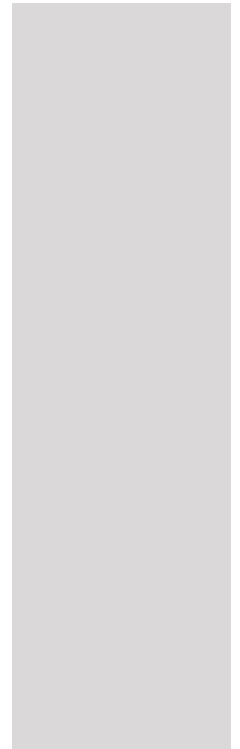
METHODOLOGY



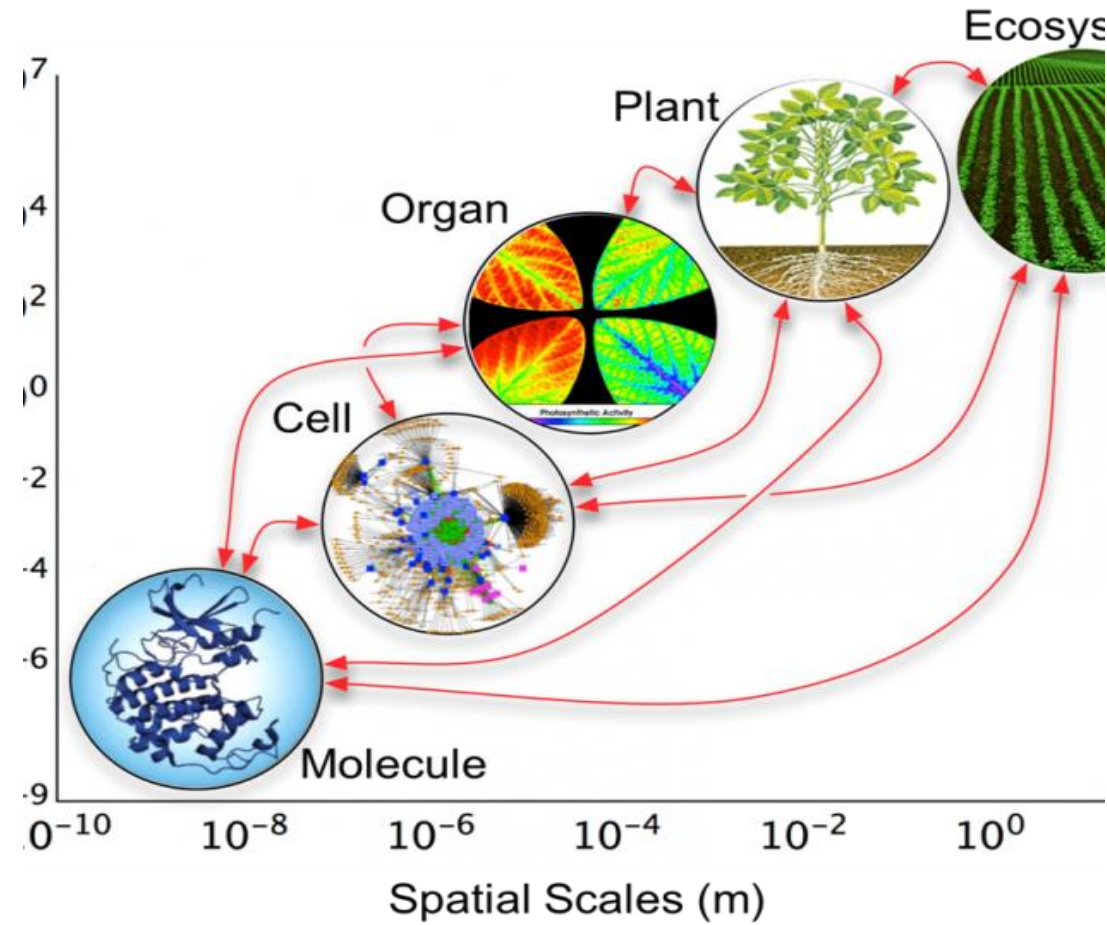
**EVALUATION
PLAN**



CONCLUSIONS

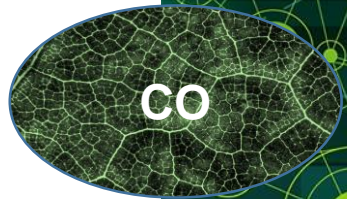


Multi-scale, multi-source, heterogeneous



(Marshall-Colon et al. 2017)

Plant phenomics datasets are in nature



«Suppose I could program my computer to create a space in which anything could be linked to anything »

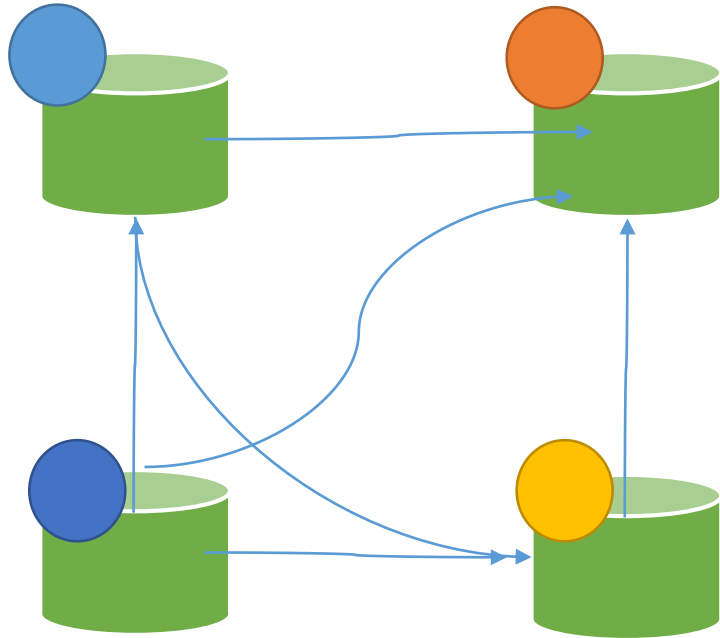
Sir Tim Berners-Lee



- PO: <http://obofoundry.org/ontology/po>
- AgrO: <http://obofoundry.org/ontology/agro>
- CO: <https://www.croponontology.org>

Plant phenomics community has adopted **Semantic Web**

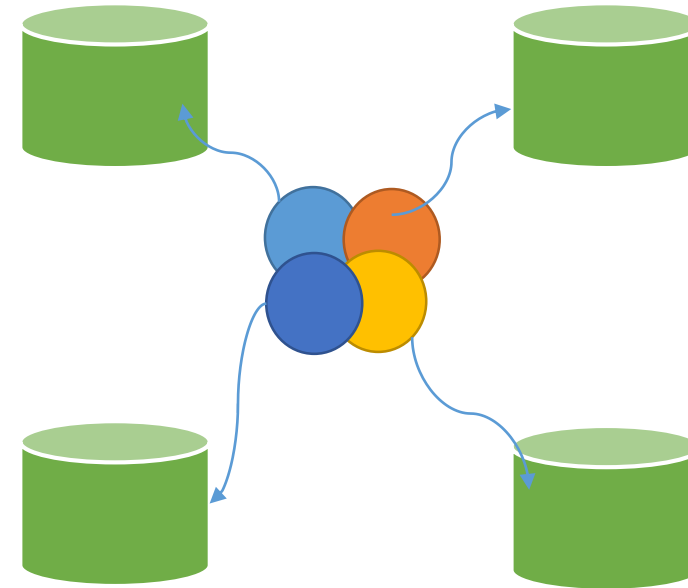
Traditional systems



- Several Apps
- Several integrations



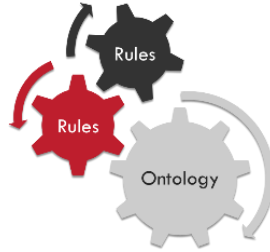
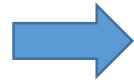
(PHIS, www.phis.inra.fr, Neveu et al., 2019)



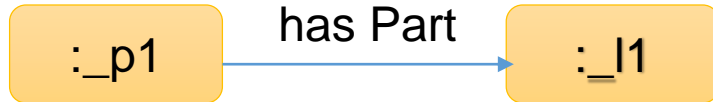
- Several Apps
- **0** integrations

PHIS, an ontology-based information system

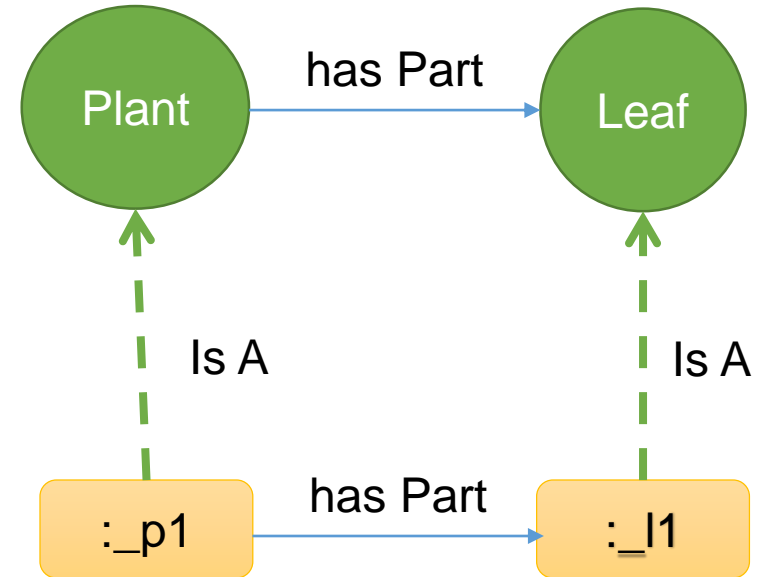
Ontologies



Facts



New facts



Reasoning services for harmonising data

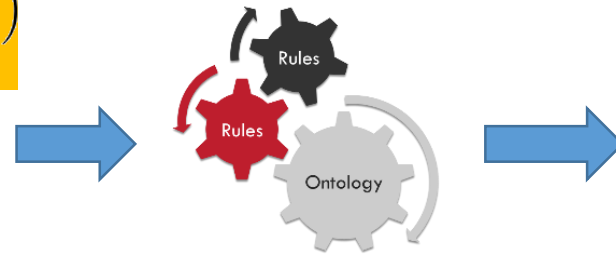


Numerous equations relate plant phenomic traits

Ontologies



$$BMI = \frac{weight}{height^2} \left(\frac{kg}{m^2} \right)$$



New facts

URI	BMI
:john	24,691358
:peter	31,1111111
:camilo	25,390625
:alexa	21,4532872
:maria	25,4693878

Facts

URI	height (m)	weight (kg)
:john	1,80	80
:peter	1,50	70
:camilo	1,60	65
:alexa	1,70	62
:maria	1,75	78

Following the reasoning logic

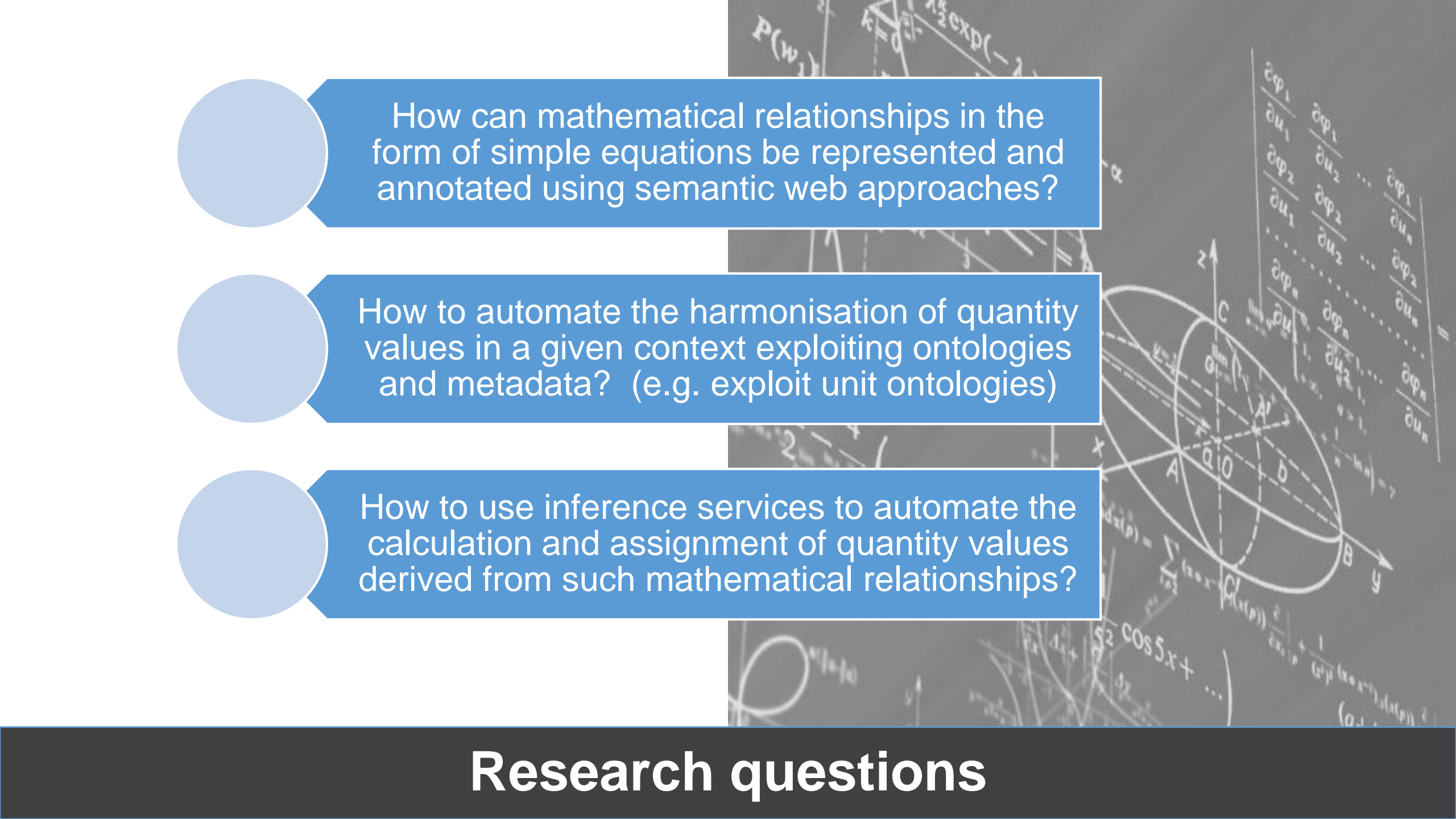
Different units

height	units
1,80	m
1,70	m
68,89	inches

OM

QUDT

Increasing the complexity

The background of the slide is a collage of mathematical content. It includes a probability density function $P(w_1)$, a Gaussian distribution formula $\frac{1}{\sigma\sqrt{2\pi}} \exp(-\frac{x^2}{2\sigma^2})$, a 3D coordinate system with axes x, y, and z, and a Hessian matrix of partial derivatives $\begin{matrix} \frac{\partial^2 \phi}{\partial u_1^2} & \frac{\partial^2 \phi}{\partial u_1 \partial u_2} & \dots & \frac{\partial^2 \phi}{\partial u_1 \partial u_n} \\ \frac{\partial^2 \phi}{\partial u_1 \partial u_2} & \frac{\partial^2 \phi}{\partial u_2^2} & \dots & \frac{\partial^2 \phi}{\partial u_2 \partial u_n} \\ \dots & \dots & \dots & \dots \\ \frac{\partial^2 \phi}{\partial u_1 \partial u_n} & \frac{\partial^2 \phi}{\partial u_2 \partial u_n} & \dots & \frac{\partial^2 \phi}{\partial u_n^2} \end{matrix}$.

How can mathematical relationships in the form of simple equations be represented and annotated using semantic web approaches?

How to automate the harmonisation of quantity values in a given context exploiting ontologies and metadata? (e.g. exploit unit ontologies)

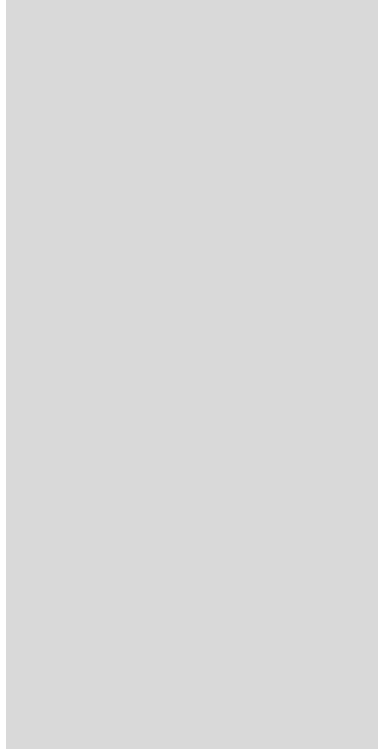
How to use inference services to automate the calculation and assignment of quantity values derived from such mathematical relationships?

Research questions

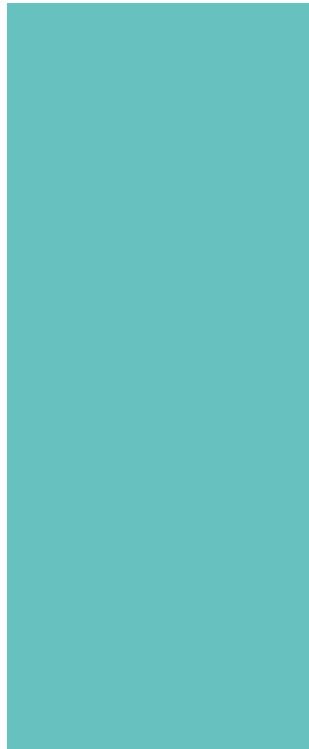


Lack of studies exploiting inference services

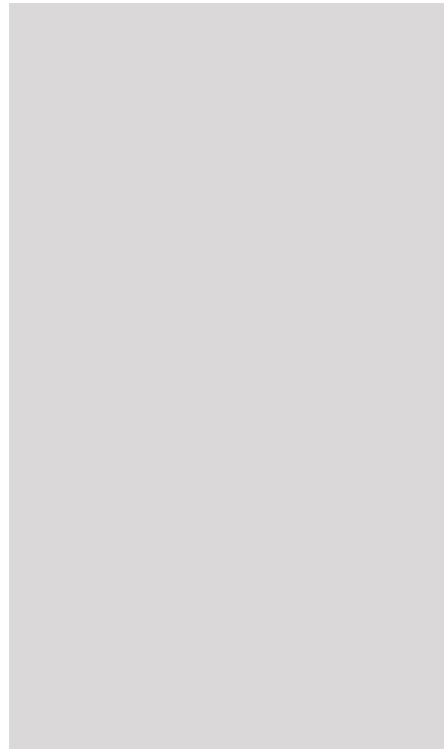
**MOTIVATION &
PROBLEM**



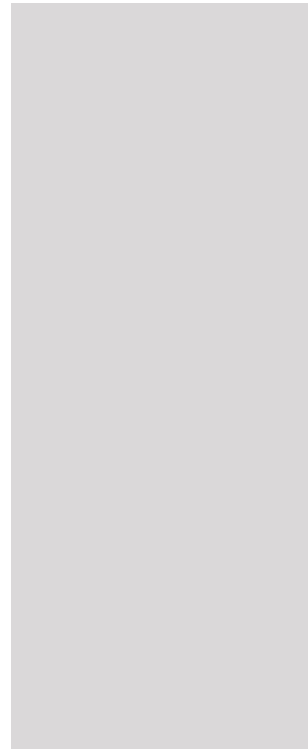
**RELATED
WORKS**



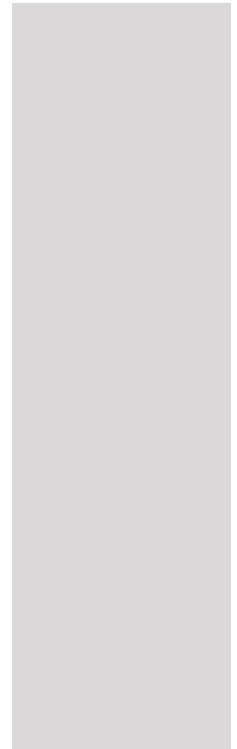
METHODOLOGY

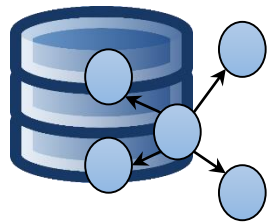


**EVALUATION
PLAN**

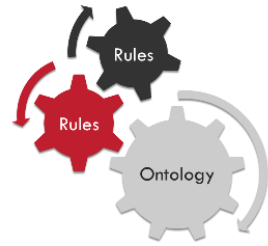


CONCLUSIONS





RDF/OWL data



Reasoning

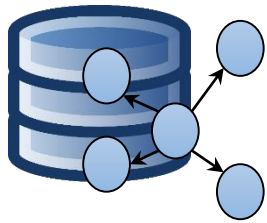


Query

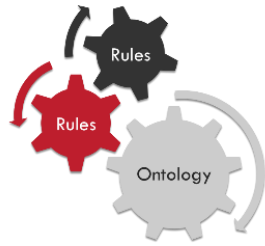
Representing and computing mathematical expressions

Ontology-based Information representation

- Function ontology (*Meester et al. 2016*)
- Unit ontologies (*OM, UO, QUDT*)
- OpenMath + RDF (*Wenzel & Reinhardt, 2012*)
- No info about how to perform the computation



RDF/OWL data



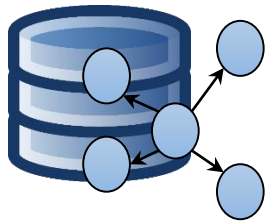
Reasoning



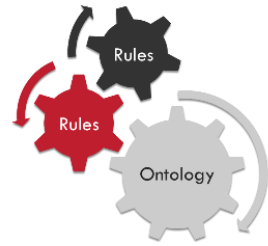
Query

Ontological reasoning

- Extend a query rewriting algorithm (*Bischof et al., 2013*),
- New datatype (*Parsia et al., 2008*)
- Semantic Web Rules (SHACL, SWRL)
- No use of unit ontologies
- Equations structured as text



RDF/OWL data



Reasoning

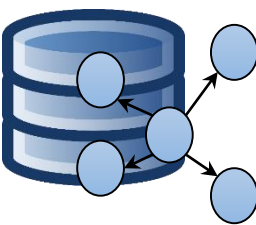


Query

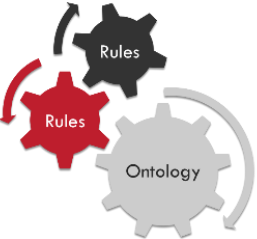
SPARQL extensions

- Query structure different from mathematical objects
- Lack of modularity
- A query is not FAIR

- Extend SPARQL functions
(Hogan et al., 2020)



RDF/OWL data



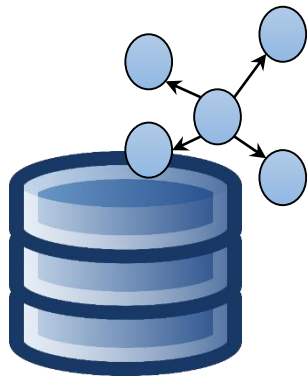
Reasoning



Query

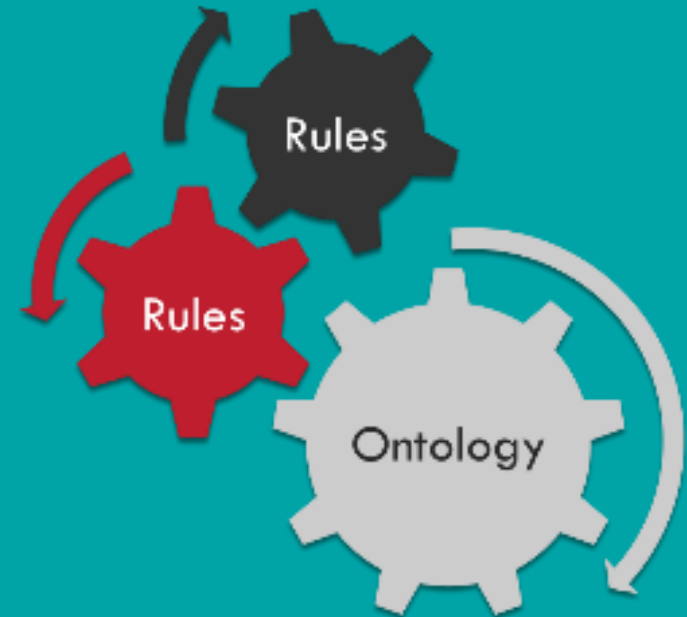
Representation features

1. FAIR equations
2. Based on ontology terms
3. Based on W3c recommendation (e.g. RDF)



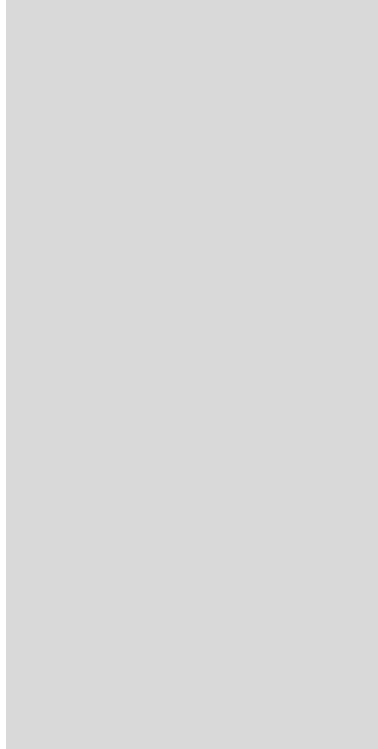
Reasoning & computation features

1. Perform equations
2. Derive new facts
3. Exploit domain ontologies (e.g. units)

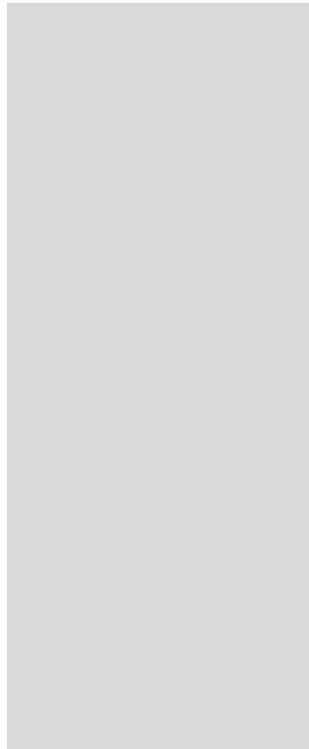


We propose an ontological framework

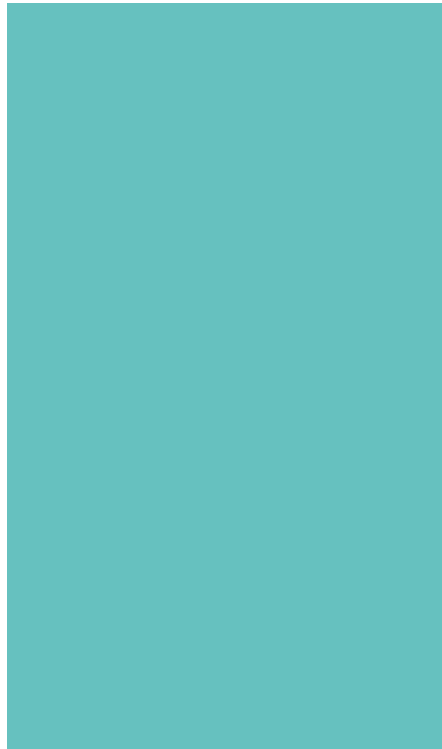
**MOTIVATION &
PROBLEM**



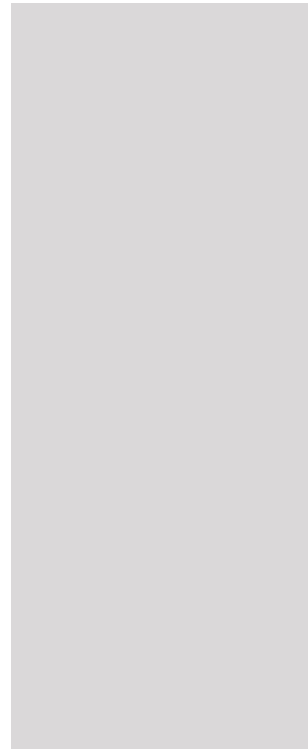
**RELATED
WORKS**



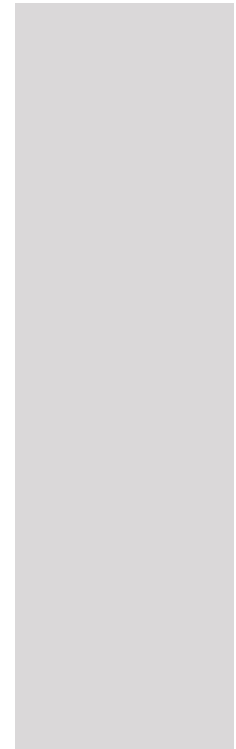
METHODOLOGY

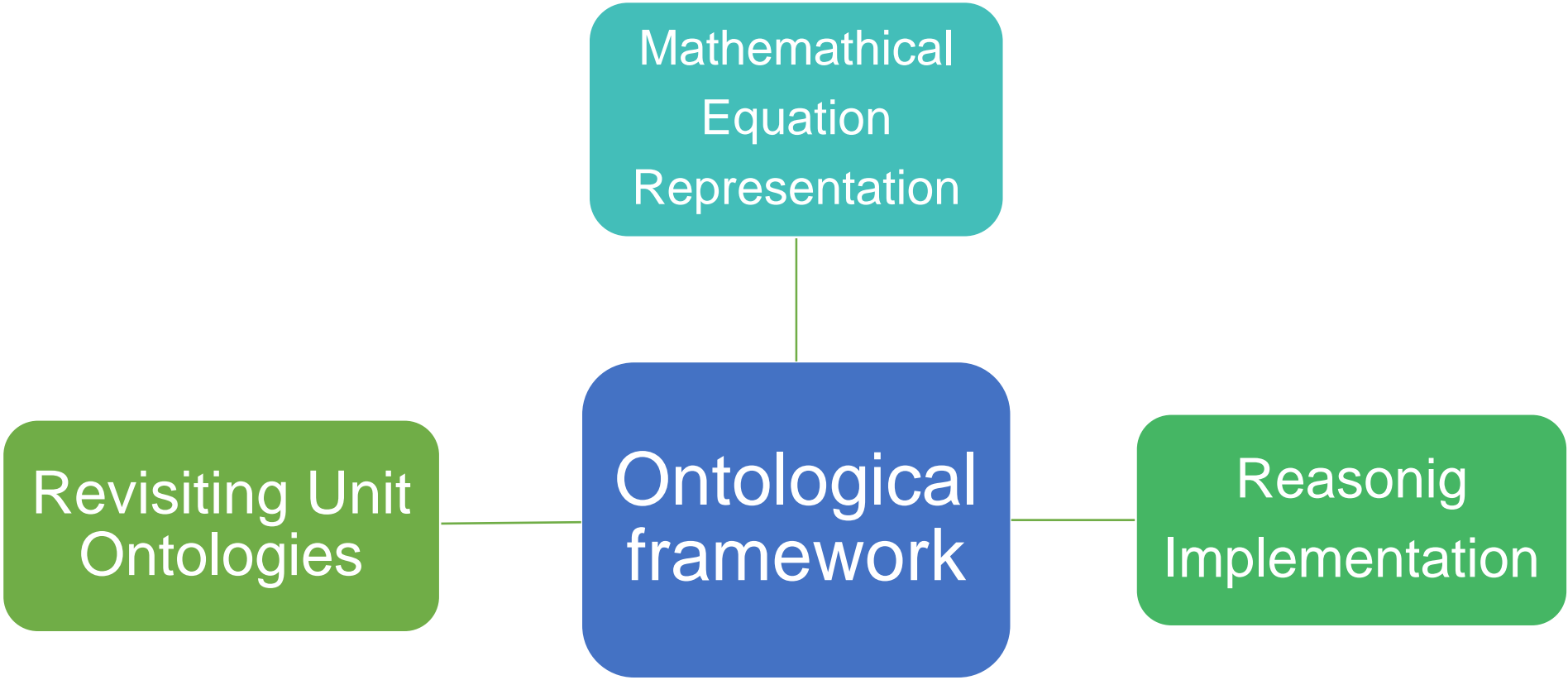


**EVALUATION
PLAN**



CONCLUSIONS





Research methodology and approach

Use metadata from unit ontologies
to infer and unify heterogeneous
measurement

**Perform Unit
Conversion**

cm → m

Normalise the temperature
observation depending on
contextual data from crops

Thermal time

Temperature → *Thermal Time*

Two case studies

Dimension units



$$1 \text{ m}^2 = 10000 \text{ cm}^2$$
$$1 \text{ cm}^2 = 1 \text{ m}^2 \times 10^{-4}$$

Light units

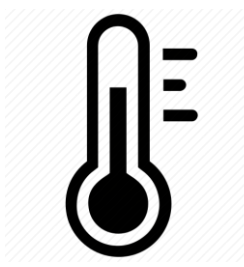
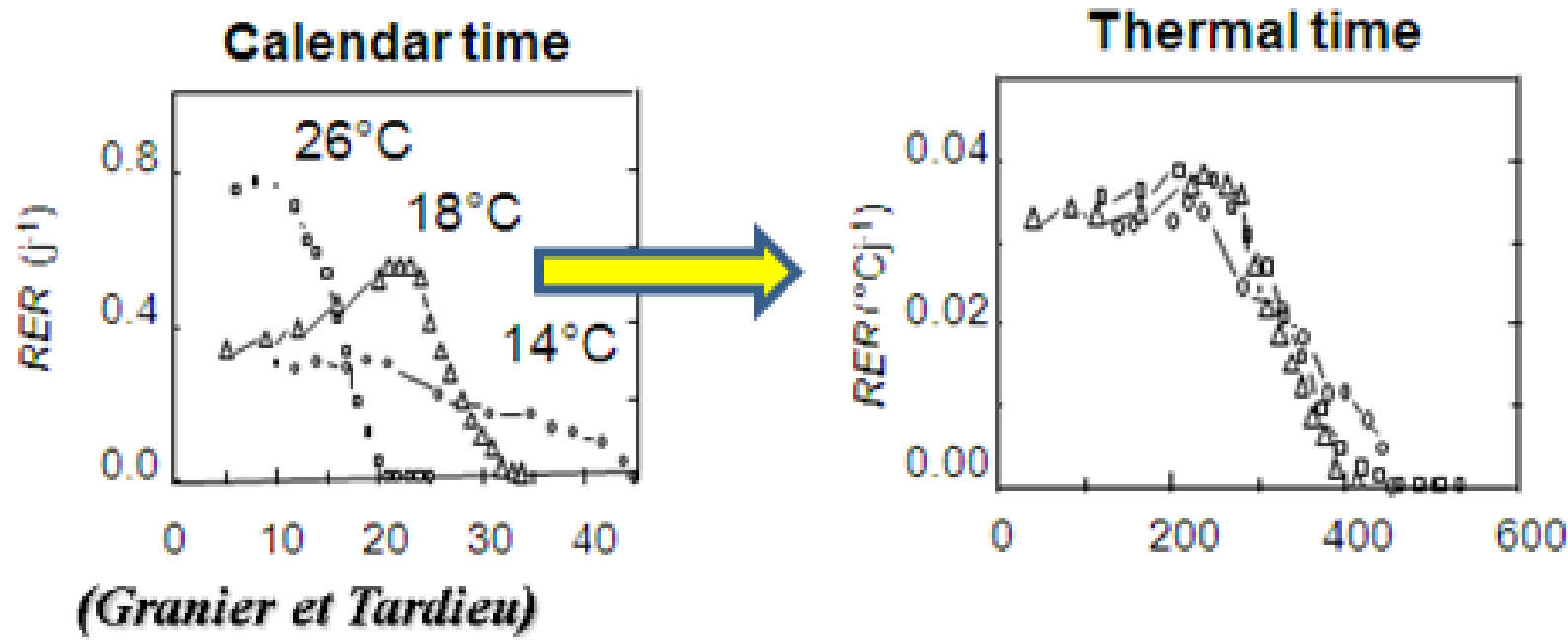


Global Solar Radiation (**Rs**)
Photosynthetically active radiation (**PAR**)

$$R_s(J \cdot \text{cm}^{-2}) \rightarrow PAR(\mu\text{mol} \cdot \text{m}^{-2}\text{s}^{-1})$$

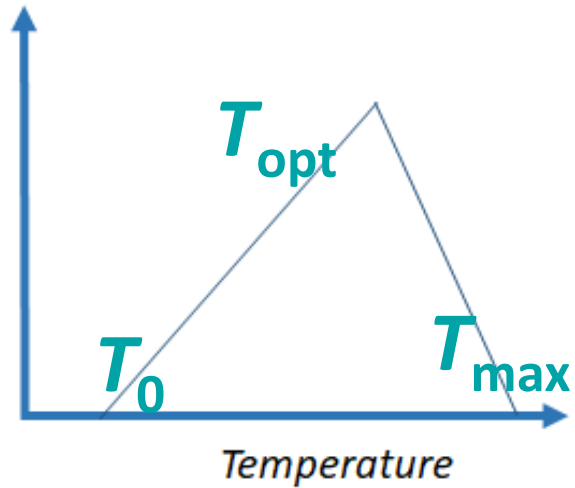
Perform unit conversion

(i.e. growing degree units) a process handled by biologists and agronomists used to normalise several temperature-dependent processes such as leaf-progression.



Thermal time definition

Bilinear Model



if $T > T_0 \leq T_{opt}$ then $T - T_0$

if $T > T_{opt} \leq T_{max}$ then $T - T_{max}$



T_{opt} 30.9 °C
 T_{max} 37.8 °C
 T_0 7 °C

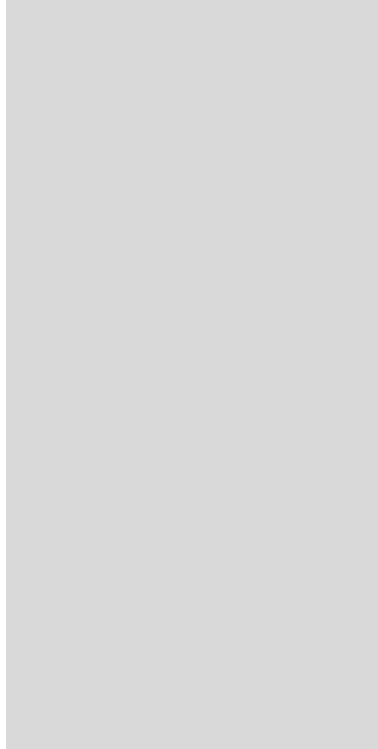


T_{opt} 31.6 °C
 T_{max} 38.9 °C
 T_0 12 °C

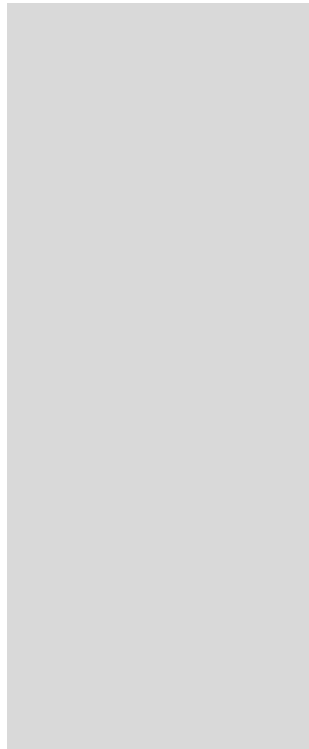


Thermal time equation

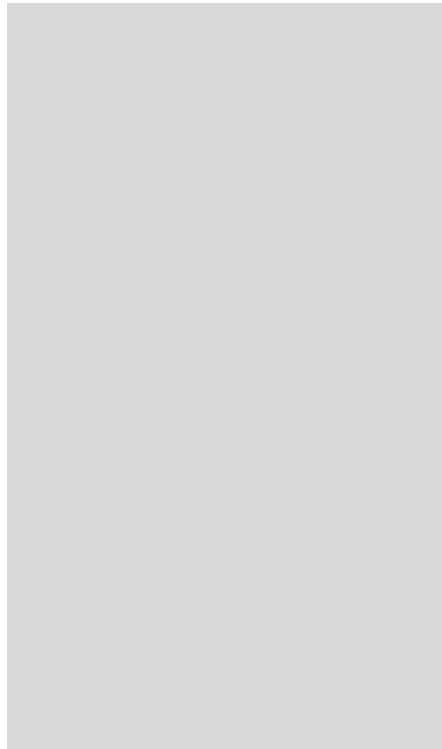
**MOTIVATION &
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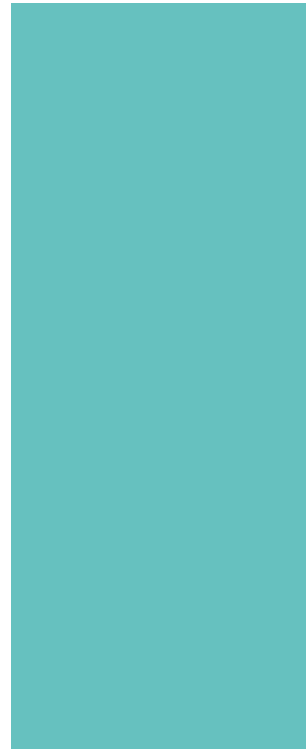
**RELATED
WORKS**



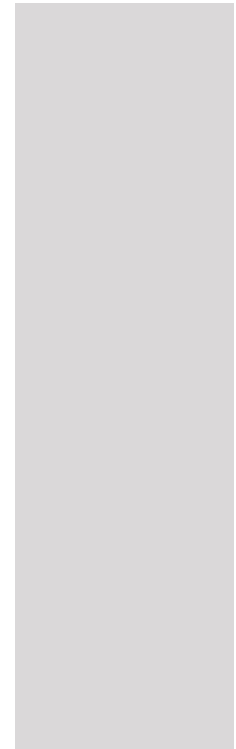
METHODOLOGY



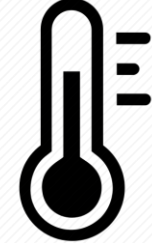
**EVALUATION
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CONCLUSIONS



Datasets



Unit ontologies

UO

OM

QUDT

Domain ontologies

PO

AgrO

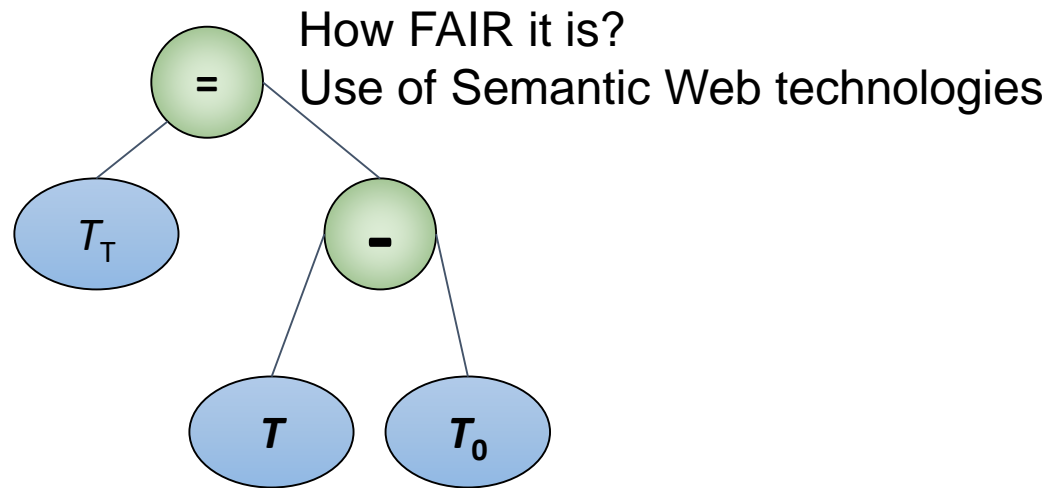
CO



16 GB RAM
1,8 GHz, 8-cores

Resources for the evaluation plan

Assessing the equation representation



Assessing the nested equation.

Thermal time

$$^{\circ}F \rightarrow ^{\circ}C$$

Assessing the unit conversion modulo

Which one is better for unit conversion?

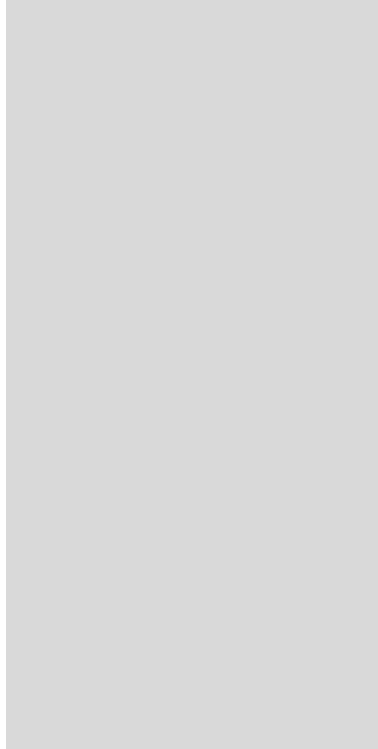
UO

OM

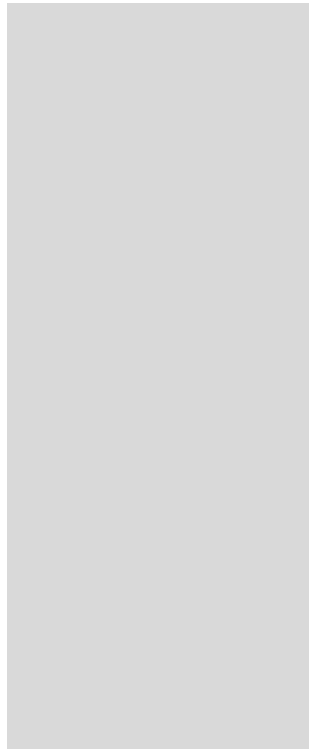
QUDT

Assesing the framework

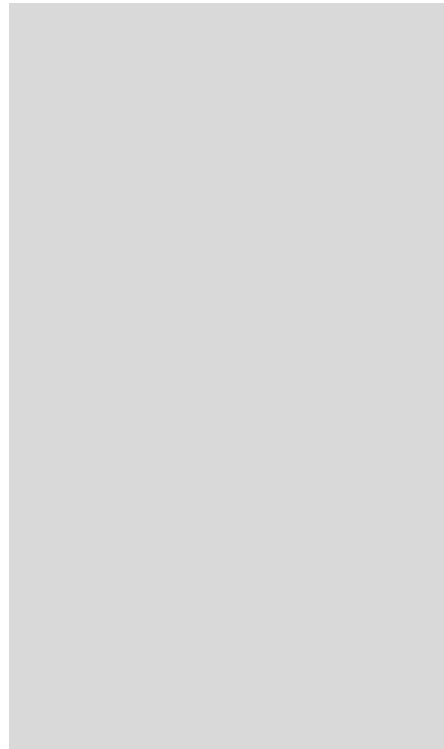
**MOTIVATION &
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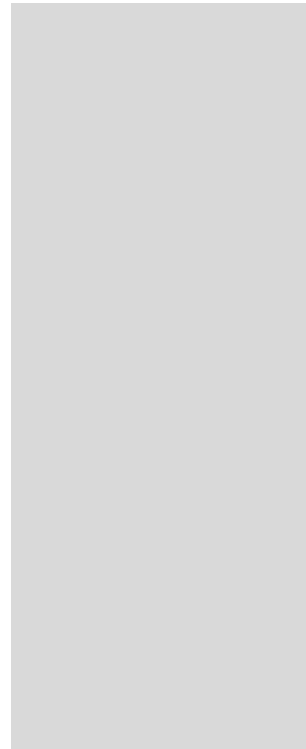
**RELATED
WORKS**



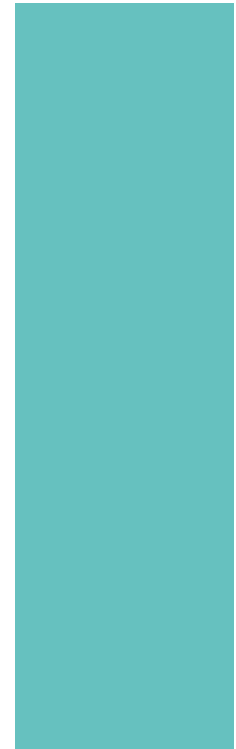
METHODOLOGY

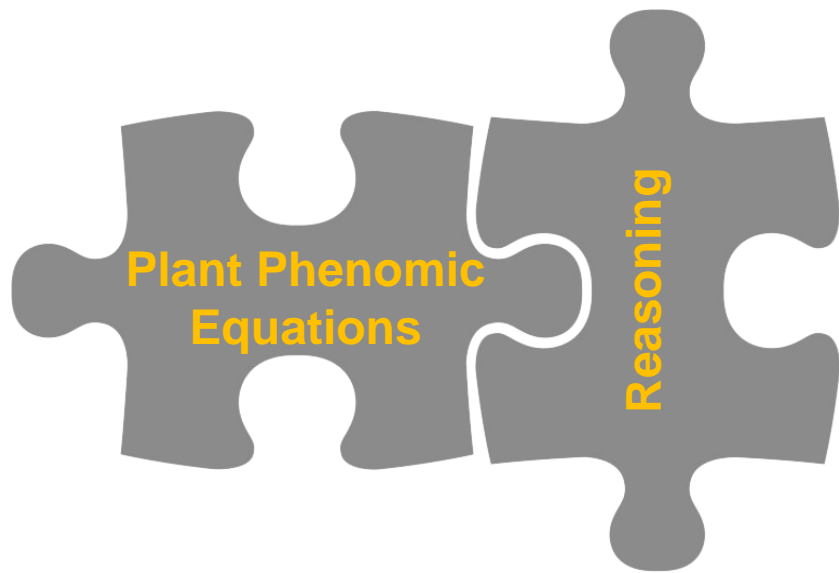


**EVALUATION
PLAN**



CONCLUSIONS





- + FAIR equations
- + Effective use of domain ontologies (units)
- + Enrich existing data with derived values

Therefore, the neglected numerical relationships will be easier to express and actionable

The framework can be used by others domains dealing with numerical attributes and mathematical equations.

Conclusions

THANK YOU

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See also: Vargas-Rojas, F. (2021, June). Ontological Formalisation of Mathematical Equations for Phenomic Data Exploitation. In *European Semantic Web Conference* (pp. 176-185). Springer, Cham.

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